

## Determining Tolerance Values of Instrumentally Measured Color Differences to Evaluate Black Filament Yarns

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### ABSTRACT

*There are many factors affecting the tolerance values of instrumentally measured color differences, including variety of industries, type of products to be matched with the original samples, the need of customers, etc. Regarding the insufficiency of various color difference formulae to deal with the acceptability of color matching of reproduced samples with the target, some researchers tried to present an instrumental color tolerance limit in accordance with the results of visual assessment experiments. Considering the specific colorimetric attributes of achromatic samples (with low lightness and chroma values), it was tried to set an instrumental tolerance limit based on the measured and visually perceived color differences between 20 filament black yarns and the reference one. The results showed that determining the color tolerance value based on various color difference formulae, i.e.  $\Delta E_{ab}^*$ , CIE94, CIE2000 and CMC (2:1), results in different instrumental wrong decisions, while the  $\Delta E_{ab}^*$  color difference equation with the color tolerance value of 0.5 for filament black yarns showed the minimum number of wrong decisions. Prog. Color Colorants Coat. 13 (2020), 187-197 © Institute for Color Science and Technology.*

### 1. Introduction

There are many industries such as textile, paper, printing, paint, automotive, ink and plastic concerning with color matching problem to quality control their colored products. The colorimetric attributes of reproduced products are controlled in two different ways; visual and instrumental [1-3]. In the case of visual color matching, the color quality control is determined by the perceived color difference between the reproduced sample and the original one [4]. There are many factors affecting the results of visual assessment experiment, including age, nationality, gender, sample size, texture, intensity and spectral quality of the light, angular size of the light source, incident angle, viewing angle, background and surround, separation and juxtaposition, interference from adjacent colors, etc. All the parameters are categorized in three main groups; i.e., observers

situation, lightening conditions and objects' properties [2, 4, 5]. Due to the subjective concept of visual assessment experiments, achieving repeatable outcomes is not simply possible. Regarding the need of different industries to quality control the color matching of reproduced batches with the target, it seems necessary to develop objective-based evaluation methods. In other words, developing an index to instrumentally evaluate the color difference values and confirm the results of visual assessment experiments leads to more reliable results [6]. In this way, various color difference equations have been employed to quantify the visually perceived color differences [7-10]. Noticeably, to pass or fail the color appearance of reproduced objects as the metameric pairs of the target, it is very important to determine an instrumental color tolerance while applying color difference formula [6, 11, 12]. Regarding the diversity of the industries, the

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variety of applied color difference equations and the customer need, the mentioned color tolerance limits are not constant and defined as arbitrary and variable values [13, 14]. On the other hand, it seems that even for a specific industry, such as textile, the other colorimetric attributes, in this case “hue”, may affect the determination of color tolerance values. It means that for the specific reproduced products in an individual industry, the samples with various hues may benefit from different color tolerance values [14, 15]. Performing the color evaluation and color acceptability process for high requested dark achromatic objects like blacks, to be reproduced and matched in textile industries is subject to many variables and proved to be difficult [15].

In contrary to ideal achromatic definition (samples with the lightness and chroma values equal to zero), actual blacks, whites and grays show low lightness and chroma properties. Regarding the tint attribute of real achromatic samples, it is not possible to suitably describe them in one-dimensional space [16-18]. Besides, the observers evaluate the color differences of real achromatic objects based on their perceived lightness and tint attribute differences [19-22]. Meanwhile, it was found that for the blackness/whiteness perception, observers decide based on their hue preferences [23-27]. While the black objects are used in different industries, i.e., textile, printing, paints, automotive, cosmetics, and so on, there are limited researches on their spectral and colorimetric properties [28-32]. Regarding the color matching of black shades one research concerned with the objective evaluation of black textile samples (both glossy and matt) in accordance with physiological experience. The results showed that the estimation of black objects' matching cannot be occurred based on the color difference values obtained from CIELAB and CMC(l:c) color difference equations and some other criteria such as  $a^*/b^*$  value and the lightness level should be concerned [15]. On the other hand, considering the insufficiency of developed color difference equations to set a manufacturing color tolerance in accordance with the visual assessment results, it was tried to derive an instrumental tolerance from the instrumental and visual dataset [4, 6]. According to this method, the  $\Delta E^*_{94}$  value that minimized the number of instrumental wrong decisions was considered as the final color tolerance value for a specific set of data.

In this paper, it is tried to drive an instrumental

color tolerance value for the black yarns based on the measured and perceived color differences. In order to avoid the effect of tint attribute, the selected samples benefit from the same tint effect in the first quarter of hue area.

## 2. Experimental

### 2.1. Sample preparation

In order to achieve an instrumental color tolerance limit based on the measured and visual perceived color differences for the black yarns, 20 filament black samples were randomly selected from different reproduced batches. Besides, the black yarn sample requested by the customer was considered as the reference. In order to prepare the opaque specimens for the instrumental measurement, 21 filament black yarns were wound closely and parallel on the uniform and neutral color cards without fluorescing agents through commercial card winders to ensure consistent tension and a constant number of 6 windings.

### 2.2. Sample measurements

The reflectance spectra of filament black yarns were measured using Color-Eye 7000A spectrophotometer (Gretag Macbeth Company) over the visible wavelength range (400 to 700 nm) by 10 nm intervals. Regarding the glossy appearance of black yarns, the specular component of the reflectance was included during the spectral measurements. The colorimetric attributes of samples in CIELAB and CIELCH color order systems were calculated under D65 standard illuminant and CIE1964 standard observer. Finally, the colorimetric differences between 20 reproduced black yarns and the reference sample were computed based on various color difference formulae; i.e.  $\Delta E^*_{ab}$ , CIE2000, CIE94 and CMC(2:1).

### 2.3. Visual assessments

In order to achieve the results of perceived color differences between the reference sample and 20 filament black yarns, the samples were evaluated under VeriVide light booth and D65 standard illuminant as pairs. 10 mature staffs, including 5 males and 5 females aged from 26 to 35 years old with an average of 30 years, evaluated the samples. The CIE1964 standard observer and the illumination/observation geometry of 0/45 were employed during the visual assessment experiments. The observers were asked to assess the

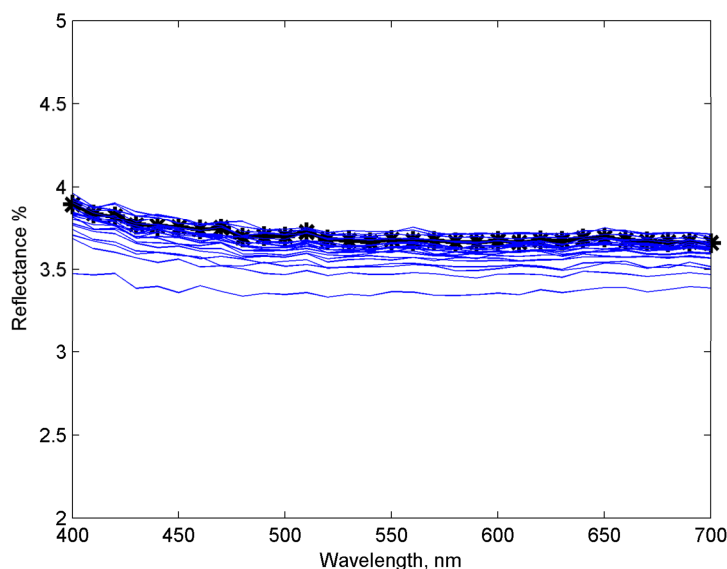
perceived color differences between the reproduced samples and the reference one as pairs and present their evaluation results by words “pass/fail”; the word “pass” means that the visually perceived color difference between the reproduced black yarns and the reference specimen is very small and acceptable within the commercial terms, while the word “fail” means that the evaluated color difference between two samples of a pair is not visually acceptable.

### 3. Results and Discussion

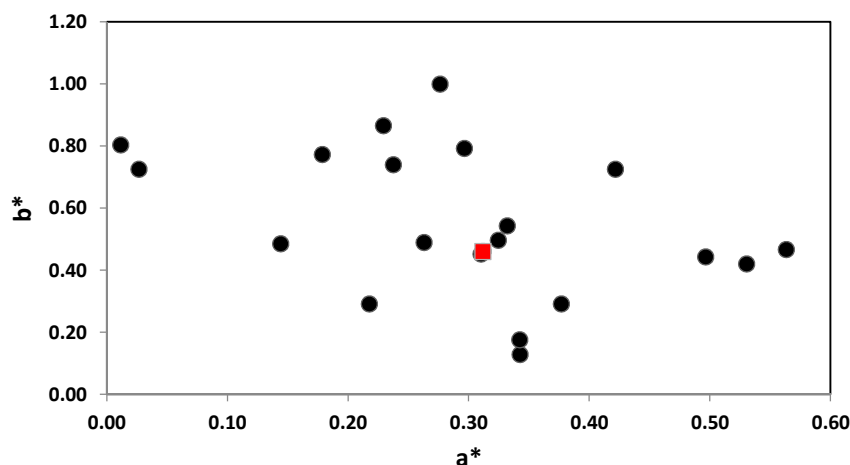
Figure 1 shows the reflectance spectra of 21 black yarns over the visible wavelength range from 400 to 700 nm. The reflectance behavior of the reference

sample is shown by the line with (\*) marker. Table 1 shows the colorimetric properties of black yarns in both CIELAB and CIELCH color spaces. The first row in Table 1 indicates the colorimetric specifications of the reference sample.

Figures 2 and 3 show the scatter plots of filament black yarns in CIELAB and CIELCH color order systems, respectively. According to Table 1 and Figure 2, all black yarns are located in the first quarter of hue area and benefit from the positive  $a^*$  and  $b^*$  values. In other words, there are some black yarns with yellowish to reddish tint attributes. The reference black yarn is shown by (■) marker.



**Figure 1:** The reflectance spectra of 21 black yarns. The (\*) marker indicates the reference sample.



**Figure 2:** Distribution of 21 black yarns over  $a^*b^*$  diagram in CIELAB color order system. The reference sample is shown by (■) marker.

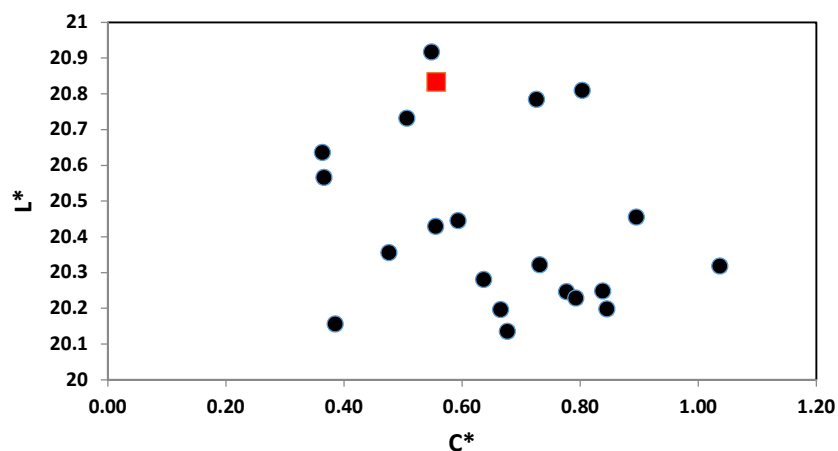
**Table 1:** The colorimetric attributes of 21 black yarns.

| Sample # | L*    | a*   | b*   | C*   | h°    |
|----------|-------|------|------|------|-------|
| Ref: d9  | 20.83 | 0.31 | 0.46 | 0.56 | 55.90 |
| d3       | 20.43 | 0.26 | 0.49 | 0.56 | 61.70 |
| d84      | 20.46 | 0.23 | 0.87 | 0.90 | 75.15 |
| d71      | 20.25 | 0.24 | 0.74 | 0.78 | 72.19 |
| d2       | 20.23 | 0.18 | 0.77 | 0.79 | 76.96 |
| d16      | 20.81 | 0.01 | 0.80 | 0.80 | 89.16 |
| d17      | 20.32 | 0.28 | 1.00 | 1.04 | 74.54 |
| d14      | 20.78 | 0.03 | 0.73 | 0.73 | 87.89 |
| d23      | 20.20 | 0.50 | 0.44 | 0.67 | 41.74 |
| d22      | 20.57 | 0.34 | 0.13 | 0.37 | 20.60 |
| d24      | 20.28 | 0.33 | 0.54 | 0.64 | 58.57 |
| d21      | 20.45 | 0.32 | 0.50 | 0.59 | 56.84 |
| d26      | 20.64 | 0.22 | 0.29 | 0.36 | 53.21 |
| d25      | 20.16 | 0.34 | 0.18 | 0.39 | 27.22 |
| d30      | 20.32 | 0.56 | 0.47 | 0.73 | 39.64 |
| d20      | 20.92 | 0.31 | 0.45 | 0.55 | 55.51 |
| d19      | 20.14 | 0.53 | 0.42 | 0.68 | 38.41 |
| d28      | 20.36 | 0.38 | 0.29 | 0.48 | 37.67 |
| d31      | 20.73 | 0.14 | 0.49 | 0.51 | 73.46 |
| d27      | 20.25 | 0.42 | 0.72 | 0.84 | 59.81 |
| d29      | 20.20 | 0.30 | 0.79 | 0.85 | 69.46 |

Figure 3 shows the C\*L\* scatter plot of 21 black yarns in CIELCH color order system. The reference black yarn is shown by (■) marker in Figure 3. According to Table 1 and Figure 3, 21 black samples benefit from low lightness and chroma values, as it is expected, while L\* values change from 20.14 to 20.92 and C\* values vary from 0.36 to 1.04.

Table 2 shows the results obtained from the visual assessment experiments. The second column in this table shows the number of observers who have visually accepted or rejected the samples of a pair. According to

Table 2, the perceived color differences between the reproduced filament black yarns and the reference sample are presented by words “pass” or “fail” under D65 standard illuminant. The word “pass” means that the majority of observers (at least 70%) did not perceive very significant color differences between the samples and the target. In fact, the perceived color differences were acceptable. On the other hand, “fail” means that at least 40% of observers have rejected the color matching between the reproduced black yarns and the target.



**Figure 3:** Distribution of 21 black yarns over C\*L\* diagram in CIELCH color order system. The reference sample is shown by (■) marker.

**Table 2:** The result of visual assessment experiments.

| Sample    | # of observers | Acceptance under D65 standard illuminant |
|-----------|----------------|------------------------------------------|
| d9 (ref.) | -              | -                                        |
| d3        | 4              | Fail                                     |
| d84       | 8              | Pass                                     |
| d71       | 7              | Pass                                     |
| d2        | 9              | Fail                                     |
| d16       | 10             | Pass                                     |
| d17       | 8              | Fail                                     |
| d14       | 10             | Pass                                     |
| d23       | 9              | Fail                                     |
| d22       | 8              | Pass                                     |
| d24       | 7              | Fail                                     |
| d21       | 9              | Pass                                     |
| d26       | 9              | Pass                                     |
| d25       | 10             | Fail                                     |
| d30       | 5              | Fail                                     |
| d20       | 10             | Pass                                     |
| d19       | 10             | Fail                                     |
| d28       | 5              | Fail                                     |
| d31       | 10             | Pass                                     |
| d27       | 7              | Fail                                     |
| d29       | 9              | Fail                                     |

Tables 3 and 4 show the lightness differences ( $\Delta L^*$ ) as well as the visual and instrumental color differences between the 20 reproduced filament black yarns and the reference sample by using various color difference equations, i.e.,  $\Delta E_{a^*b^*}$ , CIE94, CIE2000 and CMC (2:1). The first column of these tables indicates the numbers of samples that have been passed or failed in the visual assessment experiments (derived from Table

2). Table 3 shows all reproduced black yarns that have been visually accepted to have color matching with the reference sample. Table 4 indicates the reproduced black yarns that have been visually rejected.

Considering Tables 3 and 4, it is not possible to determine an instrumental color tolerance based on the employed color difference equations.

**Table 3:** The instrumental color difference values of black yarns which were visually accepted to have color matching with the reference sample.

| Pass (i #) | Sample | $\Delta E_{a^*b^*}$ | DE94 | DE2000 | CMC (2:1) | $\Delta L^*$ |
|------------|--------|---------------------|------|--------|-----------|--------------|
| 1          | d20    | 0.08                | 0.04 | 0.06   | 0.07      | 0.08         |
| 2          | d31    | 0.20                | 0.18 | 0.26   | 0.27      | -0.10        |
| 3          | d26    | 0.28                | 0.21 | 0.26   | 0.33      | -0.20        |
| 4          | d21    | 0.39                | 0.20 | 0.27   | 0.32      | -0.39        |
| 5          | d14    | 0.39                | 0.39 | 0.50   | 0.58      | -0.05        |
| 6          | d22    | 0.43                | 0.35 | 0.38   | 0.54      | -0.27        |
| 7          | d16    | 0.46                | 0.45 | 0.56   | 0.68      | -0.02        |
| 8          | d84    | 0.56                | 0.45 | 0.49   | 0.68      | -0.38        |
| 9          | d71    | 0.65                | 0.41 | 0.50   | 0.64      | -0.59        |

**Table 4:** The instrumental color difference values of black yarns which were visually rejected to have color matching with the reference sample.

| Fail (i #) | Sample | $\Delta E_{a^*b^*}$ | DE 94 | DE2000 | CMC (2:1) | $\Delta L^*$ |
|------------|--------|---------------------|-------|--------|-----------|--------------|
| 1          | d3     | 0.41                | 0.21  | 0.29   | 0.33      | -0.40        |
| 2          | d28    | 0.51                | 0.30  | 0.38   | 0.47      | -0.48        |
| 3          | d24    | 0.56                | 0.29  | 0.39   | 0.46      | -0.55        |
| 4          | d30    | 0.57                | 0.36  | 0.51   | 0.56      | -0.51        |
| 5          | d27    | 0.65                | 0.40  | 0.51   | 0.63      | -0.58        |
| 6          | d23    | 0.66                | 0.37  | 0.52   | 0.58      | -0.64        |
| 7          | d2     | 0.69                | 0.45  | 0.56   | 0.70      | -0.60        |
| 8          | d29    | 0.72                | 0.45  | 0.79   | 0.71      | -0.63        |
| 9          | d19    | 0.73                | 0.41  | 0.58   | 0.65      | -0.70        |
| 10         | d25    | 0.74                | 0.44  | 0.55   | 0.69      | -0.68        |
| 11         | d17    | 0.75                | 0.59  | 0.64   | 0.90      | -0.51        |

Samples in Tables 3 and 4 have been sorted into “pass” and “fail” and placed in ascending order based on their instrumental  $DE_{a^*b^*}$  with the reference sample. Similar tables were designed for other employed color differences;  $DE_{94}$ ,  $DE_{2000}$  and  $DE_{CMC}(2:1)$ , while they were not shown here. Then, the cumulative percentages of each group of “passed” or “failed” pairs were calculated based on Equations 1 and 2 [4].

$$\text{Cumulative}_{\text{pass},i} = 100(i/n_{\text{pass}}) \quad (1)$$

$$\text{Cumulative}_{\text{fail},i} = 100-100(i/n_{\text{fail}}) \quad (2)$$

where  $n_{\text{pass}}$  and  $n_{\text{fail}}$  represent the number of black yarns passed or failed, respectively, to be matched with the reference sample, and  $i$  refers to black yarns 1, 2, ...,  $n_{\text{pass}}/n_{\text{fail}}$ .

In order to determine an instrumental color tolerance value for black filament yarns, the ascending ordered color difference values are shown in Table 5

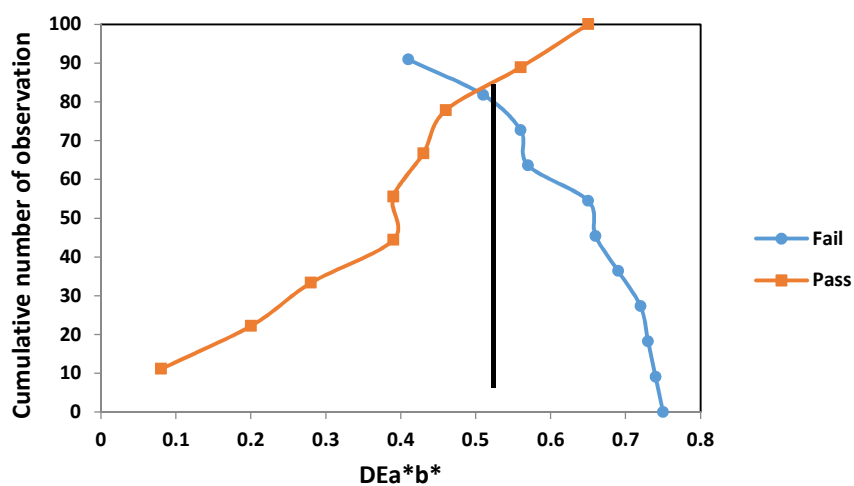
with their corresponding cumulative percentages [4]. The left side of Table 5 shows the cumulative percentages corresponding to the ordered color difference values of passed samples. The cumulative percentages corresponding to the ordered color difference values of failed samples are shown in the right side of Table 5.

The computed cumulative percentages were plotted against the ordered color difference values. Figures 4 to 7 show various color difference versus their corresponding cumulative percentages for two groups of data (“pass/fail”). In all the figures, the optimized tolerance value is defined by the intersection point of two data sets.

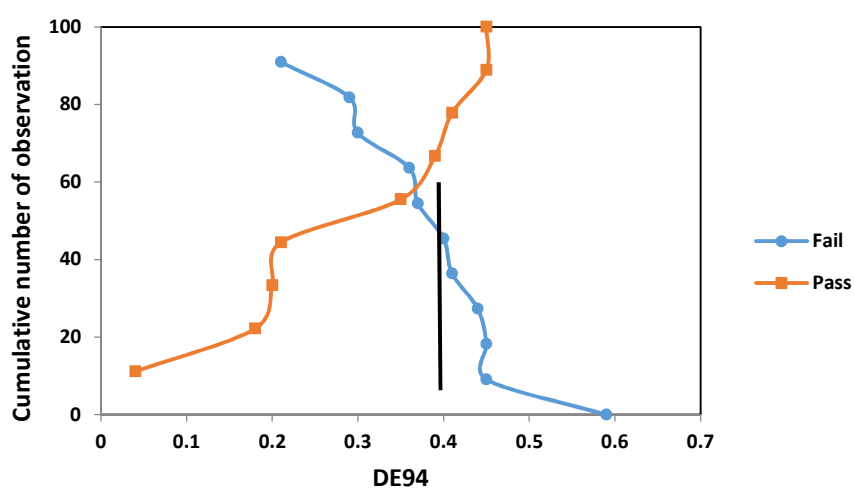
According to the intersection point shown in Figure 4, the color difference value that minimizes the number of instrumental wrong decisions is 0.5 for  $DE_{a^*b^*}$ . Based on the achieved tolerance value of (0.5  $DE_{a^*b^*}$ ), the number of instrumental wrong decisions is 3 for these data.

**Table 5:** The cumulative percentages of the ascending ordered color difference values

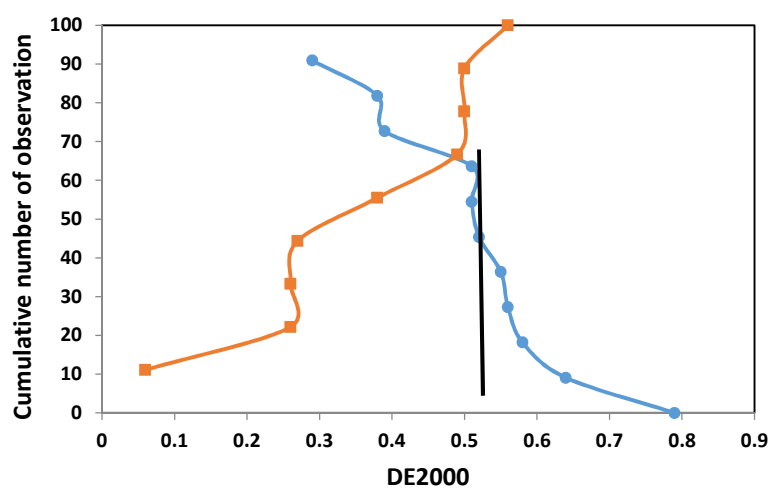
| Pass<br>Cumulative% | $DE_{a^*b^*}$ | $DE_{94}$ | $DE_{2000}$ | $CMC2:1$ | Fail<br>Cumulative<br>% | $DE_{a^*b^*}$ | $DE_{94}$ | $DE_{2000}$ | $CMC2:1$ |
|---------------------|---------------|-----------|-------------|----------|-------------------------|---------------|-----------|-------------|----------|
| 11.1                | 0.08          | 0.04      | 0.06        | 0.07     | 90.9                    | 0.41          | 0.21      | 0.29        | 0.33     |
| 22.2                | 0.20          | 0.18      | 0.26        | 0.27     | 81.8                    | 0.51          | 0.29      | 0.38        | 0.46     |
| 33.3                | 0.28          | 0.20      | 0.26        | 0.32     | 72.7                    | 0.56          | 0.3       | 0.39        | 0.47     |
| 44.4                | 0.39          | 0.21      | 0.27        | 0.33     | 63.6                    | 0.57          | 0.36      | 0.51        | 0.56     |
| 55.5                | 0.39          | 0.35      | 0.38        | 0.54     | 54.5                    | 0.65          | 0.37      | 0.51        | 0.58     |
| 66.7                | 0.43          | 0.39      | 0.49        | 0.58     | 45.4                    | 0.66          | 0.4       | 0.52        | 0.63     |
| 77.8                | 0.46          | 0.41      | 0.50        | 0.64     | 36.4                    | 0.69          | 0.41      | 0.55        | 0.65     |
| 88.9                | 0.56          | 0.45      | 0.50        | 0.68     | 27.3                    | 0.72          | 0.44      | 0.56        | 0.69     |
| 100                 | 0.65          | 0.45      | 0.56        | 0.68     | 18.2                    | 0.73          | 0.45      | 0.58        | 0.70     |
| -                   | -             | -         | -           | -        | 9.1                     | 0.74          | 0.45      | 0.64        | 0.71     |
| -                   | -             | -         | -           | -        | 0                       | 0.75          | 0.59      | 0.79        | 0.90     |



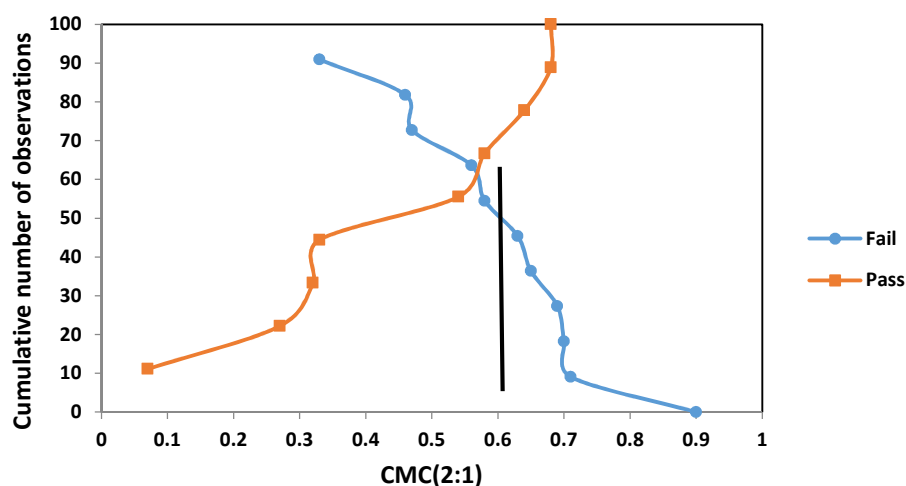
**Figure 4:** The cumulative percentages corresponding to ordered DE a\*b\* color difference values.



**Figure 5:** The cumulative percentages corresponding to ordered DE94 color difference values.



**Figure 6:** The cumulative percentages corresponding to ordered DE2000 color difference values.



**Figure 7:** The cumulative percentages corresponding to ordered DECMC 2:1 color difference values.

**Table 6:** The number of instrumental wrong decisions as well as the achieved tolerance limits corresponding to the applied color difference formulae.

| Color difference formula | Tolerance value | # Instrumental wrong decisions |
|--------------------------|-----------------|--------------------------------|
| DEa*b*                   | 0.5             | 3                              |
| DE94                     | 0.37            | 8                              |
| DE2000                   | 0.49            | 6                              |
| DECMC(2:1)               | 0.57            | 8                              |

Table 6 summarizes the results achieved from Figures 4 to 7 based on the achieved tolerance values corresponding to the applied color difference formulae. Although the scale of CIELAB color difference formula is not the same as the visual perception of color differences, according to Table 6, the DEa\*b\* color difference equations with the tolerance value of 0.5 result in the minimum number of instrumental wrong decisions (3) among all applied color difference formulae. Besides, the DE94 and CMC (2:1) with the maximum number of instrumental wrong decisions (8) represent the tolerance values of (0.37) and (0.57), respectively.

The acquired color tolerance values could be considered for the final agreement between the clients and the suppliers of black textile products. It is noticeable that although the CIELAB color difference formula was found as the best, the achieved results are

based on the judgment of perceived color differences between 20 samples and a single target. Regarding the mentioned limitation and the number of observers, some further work and research should be done for achieving more reliable results.

#### 4. Conclusion

At the present study, deriving an instrumental color tolerance limit was investigated for filament black yarns using a set of color difference formulae. In this way, the subjective and objective color evaluations were performed between 20 reproduced filament black yarns and a target. 10 mature observers subjectively assessed the color matching of samples as pairs. Besides, four color difference formulae, i.e., DEa\*b\*, DE94, DE2000 and CMC(2:1), were employed to objectively evaluate the color differences. The results showed that DEa\*b\* color difference formula with the

tolerance value of 0.5 results in the minimum number of instrumental wrong decisions among all applied color difference equations. This limit value facilitates

the management of product color appearance and can be used to control the acceptance of the color differences achieved between the sample and the target.

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